GRESHAM PRIMARY SCHOOL CALCULATION POLICY April 2024

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Signed by:

Headteacher

Date:

Chair of governors

Date:

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STATEMENT OF INTENT

This calculation policy has been written in line with the programmes of study taken from the revised National Curriculum for Mathematics. It provides guidance on appropriate calculation methods and progression. The content shows progression between years under the following headings: addition, subtraction, multiplication and division.

Gresham's maths curriculum (available on the school website) also highlights the progression between these key skills and when they will be introduced and taught.

Children will use mental methods as their first port of call when appropriate, but for calculations that they cannot do in their heads, they will need to use an efficient written method accurately and with confidence.

This policy is design to support both educators and parents in supporting children's understanding and application of calculation.

The emphasis, initially, is on mental calculations skills, but progresses to the written strategies that your child is expected to become familiar with. Whilst this document has been organised into the expected outcomes for each year group, it is important to recognise that children develop their mathematical skills at different rates and that you should work with your child, using a combination of practical, mental and written activities, at a level that is suitable to them.

With this said, it is also important to recognise that the maths curriculum aims to develop reasoning and problem-solving skills. These are developed through carefully planned lessons and home learning and also the result of children adhering to the content of their year group. Children who are highly proficient at maths will be challenged appropriately, but always through extending their knowledge of the content for their year group. Rapid progression through the curriculum does not allow for a clear mathematical understanding of what is 'happening' and whilst children can remember rules and patterns, they will not develop their problem solving and reasoning skills.

AIMS OF THE POLICY

- To ensure consistency and progression in our approach to calculation.
- To ensure that children develop an efficient, reliable, formal written method of calculation for all operations.
- To ensure that children can use these methods accurately with confidence and understanding.
- To give parents/carers the confidence to support children in maths at home.

CPA (Concrete, Pictorial, Abstract)

As a result of an overview of the National Curriculum, in 2013 there was a shift in focus. The term 'mastery' was introduced following the success of programmes such as Shanghai Maths and Singapore Maths.

Mastery refers to children acquiring a deep-rooted and secure understanding of maths. Children are introduced to a concept and once embedded they are then encouraged to rationalise and reason. This promotes a deeper understanding and moves away from children having to learn by rote.

With maths mastery in mind, schools will typically use some variation of the CPA approach.

CPA stands for:

- Concrete
- Pictorial
- Abstract

The CPA approach underpins the aims of the National Curriculum. Historically, there has perhaps been a tendency to show progression in maths by rapidly moving children from topic to topic. However, this can lead to a superficial understanding where children rely on learning by rote or following rules or patterns to achieve success. It does not lend itself to gaining a deep understanding.

CPA focuses on the three key stages of mathematical learning and show how children are taught to build upon existing knowledge.

Concrete refers to the physical objects that children may use to count and order. These could be counters, cubes or other physical apparatus. This physical representation of a number helps children to 'see' what is happening when they are calculating.

Physical representations follow this. This will include children starting to use number-lines, times tables grids, hundred squares and similar. The children have a secure understanding of number and are now able to represent it visually, without needing physical objects in front of them.

Abstract is the final stage. At this point children are very secure and familiar with number and can now use written methods to calculate. This will involve more traditional written methods including the column method for addition, subtraction and multiplication and long and short division. Children will be able to explain how these methods work as throughout their time at primary school they will be encouraged to make links between the three stages.

It is of paramount importance to allow children to progress through these stages equally. Abstract written methods are generally introduced and taught in KS2 where they have spent the majority of EYFS and KS1 focussing on concrete and pictorial examples.

Children who are introduced to abstract concepts too early, without a secure grasp of the concrete and pictorial stages can result in children 'learning by rote' where they can remember a set of rules to find an answer, but they cannot explain how or why their answer is correct.

The following pages offer visual examples of how the four operations (addition, subtraction, multiplication and division) are taught throughout Gresham.

Early Years

A key priority of any Primary School maths curriculum is to ensure that children develop a strong sense of number and place value. Children will continually encounter numbers in the world around them. The ability to recognise the symbol 5, and name it, is very different from understanding the 'fiveness' of it, and it is the development of this latter skill that is crucial to a child's mathematical ability.

Furthermore, it is important to recognise that just because a child can recite number names in order, does **not** necessarily mean that they can count. As with learning the alphabet, children can recall a sequence of numbers by rote without any real grasp or understanding of what they mean (hence young children often omit numbers as they count). Gaining familiarity with number names through songs and rhymes is of course helpful, but emphasis should be placed on helping children make links between these number names and the number of objects they equate to.

In the Foundation Stage, as well as teaching the children to count objects, significant attention is given to cultivating number recognition and the development of mental representations. In order to do this, much of their experience with number play in the early years will involve concrete, movable objects. In the Foundation Stage, this secure knowledge of number and place value underpins all calculation that may be taught later in children's school lives.

Constant repetition, embedding and teaching of these key skills ensure the children's deep understanding of number and in the Foundation Stage this can be taught in a number of ways including:

- Writing numbers
- Accurate 1-1 correspondence (touch it, move it, count it).
- A secure understanding of 'what' a number is.
- Recognising numbers visually.
- Use of concrete materials (Dienes and numicon)
- Counting forwards and backwards through a number-line.

The school utilises the White Rose Scheme for maths.

Addition

Below outlines the progressive steps within addition, alongside the representations and models used to teach these.

Skill	Year	Representation and Models*			
Add two 1-digit numbers to 10	1	Part-whole model Bar	Ten frames (within 10)		
		model Number shapes	Bead strings (10) Number		
			tracks		
Add 1 and 2-digit numbers to 20	1	Part-whole model Bar	Bead strings (20) Number		
		model Number shapes	tracks Number lines		
		Ten frames (within 20)	(labelled) Straws		
Add three 1-digit numbers	2	Part-whole model Bar	Ten frames (within 20)		
		model	Number shapes		
Add 1 and 2-digit numbers to 100	2	Part-whole model Bar	Number lines (blank)		
		model Number lines	Straws Hundred square		
		(labelled)			
Add two 2-digit numbers	2	Part-whole model Bar	Base 10 Place value		
		model Number lines	counters		
		(blank) Straws			
Add with up to 3-digits	3	Part-whole model Bar	Base 10 Place value		
		model	counters Column addition		
Add with up to 4-digits	4	Part-whole model Bar	Base 10 Place value		
		model	counters Column addition		
Add with more than 4 digits	5	Part-whole model Bar	Place value counters		
		model	Column addition		
Add with up to 3 decimal places	5	Part-whole model Bar	Place value counters		
		model	Column addition		

Skill: Add 1-digit numbers within 10	Year 1
	When adding numbers to 10, children can explore both aggregation and
	augmentation. The part- whole model, discrete and continuous bar model,
4 + 3 = 7	frame support aggregation. The
	combination bar model, ten frame, bead string and
	number track all support augmentation.
Skill: Add 1 and 2 -digit numbers to 20	Year 1
	When adding one - digit numbers that cross 10, it is important to highlight the importance of ten ones equalling one ten. In Year 1, this is only done
8 + 7 = 15	just by counting on. From Year 2, use different manipulatives can be used
	to represent this exchange alongside number lines to support children in
	understanding how to partition their jumps.









Subtraction

Below outlines the progressive steps within subtraction, alongside the representations and models used to teach these.

Skill	Year	Representation and Models				
Subtract two 1-digit numbers to	1	Part-whole model Bar model	Ten frames (within 10)			
10		Number shapes	Bead strings (10) Number			
			tracks			
Subtract 1 and 2-digit numbers	1	Part-whole model Bar model	Bead string (20) Number			
to 20		Number shapes Ten frames	tracks Number lines			
		(within 20)	(labelled) Straws			
Subtract 1 and 2-digit numbers	2	Part-whole model Bar model	Number lines (blank)			
to 100		Number lines (labelled)	Straws Hundred square			
Subtract two 2-digit numbers	2	Part-whole model Bar model	Base 10 Place value			
		Number lines (blank) Straws	counters			
Subtract with up to 3- digits	3	Part-whole model Bar model	Base 10 Place value			
			counters Column			
			subtraction			
Subtract with up to 4- digits	4	Part-whole model Bar model	Base 10 Place value			
			counters Column			
			subtraction			
Subtract with more than 4 digits	5	Part-whole model Bar model	Place value counters			
			Column subtraction			
Subtract with up to 3 decimal	5	Part-whole model Bar model	Place value counters			
places			Column subtraction			









Multiplication – Times Tables

Below outlines the progressive steps within times tables, alongside the representations and models used to teach these.

Skill	Year	Representation	n and Models*
Recall and use multiplication	2	Bar model Number shapes	Ten frames Bead strings
and division facts for the 2-		Counters Money	Number lines Everyday
times table			objects
Recall and use multiplication	2	Bar model Number shapes	Ten frames Bead strings
and division facts for the 5-		Counters Money	Number lines Everyday
times table			objects
Recall and use multiplication	2	Hundred square Number	Ten frames Bead strings
and division facts for the 10-		shapes Counters Money	Number lines Base 10
times table			
Recall and use multiplication	3	Hundred square Number	Bead strings Number lines
and division facts for the 3-		shapes Counters	Everyday objects
times table			
Recall and use multiplication	3	Hundred square Number	Bead strings Number lines
and division facts for the 4-		shapes Counters	Everyday objects
times table			
Recall and use multiplication	3	Hundred square Number	Bead strings Number tracks
and division facts for the 8-		shapes	Everyday objects
times table			
Recall and use multiplication	4	Hundred square Number	Bead strings Number tracks
and division facts for the 6-		shapes	Everyday objects
times table			
Recall and use multiplication	4	Hundred square Number	Bead strings Number lines
and division facts for the 7-		shapes	
times table			
Recall and use multiplication	4	Hundred square Number	Bead strings Number lines
and division facts for the 9-		shapes	
times table			
Recall and use multiplication	4	Hundred square Base 10	Place value counters
and division facts for the 11-			Number lines
times table			
Recall and use multiplication	4	Hundred square Base 10	Place value counters
and division facts for the 12-			Number lines
times table			

Skill: 2 times table	Year 2
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	Encourage daily counting in multiples both forwards and backwards. This can be supported using a
	number line or a hundred square. Look for patterns in the two times table, using
1 2 3 4 5 6 7 8 9 9 11 13 14 15 6 17 19 20 21 22 23 25 29 29 29 30 31 33 35 39 39 40 41 43 45 47 49 65	to support. Notice how all the numbers are even and there is a pattern in the ones. Use different
	fluency.
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20	
Skill: 5 times table	Year 2
Skill: 5 times table 0 5 10 15 20 25 30 35 40 45 50 55 60	Year 2 Encourage daily counting in multiples both forwards and
Skill: 5 times table	Year 2 Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the five times table, using
Skill: 5 times table Skill: 5 times table O 1 2 3 4 0 6 7 8 9 0 1 2 3 4 6 7 8 9 0 0	Year 2 Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the five times table, using concrete manipulatives to support. Notice the pattern in the ones as well as highlighting the odd, even, odd, even pattern.

Skill: 10 times table	Year 2
0 10 20 30 40 50 60 70 80 90 100	Encourage daily counting in multiples both forwards and
	backwards. This can be supported using a number line or a hundred square. Look for patterns in the ten times table, using concrete manipulatives to support. Notice the pattern in the digits - the ones are always 0, and the tens increase by 1 ten each time.
Skill: 3 times table	Year 3
	Encourage daily counting in multiples both forwards and backwards. This can be
$\frac{1}{12} \xrightarrow{3} 4 \xrightarrow{5} \xrightarrow{6} 7 \xrightarrow{8} \xrightarrow{9} 10}{13 14} \xrightarrow{9} 16 \xrightarrow{17} \xrightarrow{9} 19 20} \xrightarrow{13} 32 \xrightarrow{3} 34 \xrightarrow{35} 39 \xrightarrow{37} 38 \xrightarrow{39} 40} \xrightarrow{14} 32 \xrightarrow{34} 35 \xrightarrow{36} 37 \xrightarrow{7} 38 \xrightarrow{39} 40} \xrightarrow{3} 3 \xrightarrow{6} 9 \xrightarrow{12}$	number line or a hundred square. Look for patterns in the three times table, using concrete manipulatives to support. Notice the odd, even, odd, even pattern using number shapes to support.
++++++++++++> 0 3 6 9 12 15 18 21 24 27 30 33 36	Highlight the pattern in the ones using a hundred square.



		C	skill• 6 +i	imes table	<u>ــــــــــــــــــــــــــــــــــــ</u>								Year <i>1</i>
		-						-	a	-			Encourage daily
	+++	H	11		1	0	3 4	5	16	17 (8	9 20	counting in multiples.
			_		21	22	23 62	25	26	27	28 2	9 00	supported by a number
					31	32	33 34	35	3	37	38 3	9 40	line or a hundred
				:::	41	(42)	43 44	45	46	47 (4B) 4	9 50	square. Look for
	45 0-88	12.088	120	-0.4	51	52 1	53 64	55	56	57 1	58 5	9 😡	patterns in the six times
6	12	18	24	30	61	62	63 64	65	66	67 (68 6	9 70	table, using
0	12	10	24	50	71	72	73 74	75	76	77	78 7	9 80	manipulatives to
36	42	48	54	60	81	82 1	83 84	85	86	87 1	88 8	9 90	support. Make links to
66	72	78	84	90	91	92	93 94	95	96	97 9	98 9	9 100	the 3 times table, seeing
-					0 - A				92 MP		- 22	410 - 55	how each multiple is
							a catalog						uouble the threes.
	000) - 0	000	\propto)	\propto	X	∞	\bigcirc	\supset	_	ones within each group
					1000								of five multiples
													Highlight that all the
	\vdash	++	-	+++	\vdash	-	\vdash		+	+	\rightarrow		multiples are even using
	0 6	12 18	3 24 3	0 36 4	2 48	B 5	4 6	0 6	6	72			number shapes to
													support.
		S	Skill: 9 ti	imes table	е								support. Year 4
		S	Skill: 9 ti	imes table	1	2	3 4	5	6	7	8	9 10	support. Year 4 Encourage daily
		5	Skill: 9 ti	imes table		2	3 4	4 15	6	7	8) 10 19 20	support. Year 4 Encourage daily counting in multiples
		2	Skill: 9 ti	imes table	1	2 12 22	3 4 13 1 23 2	4 5 4 15 4 25	6 16 26	? 17	8 () 10 19 20 29 30	support. Year 4 Encourage daily counting in multiples both forwards and
		2	Skill: 9 ti	imes table	1 11 21 31	2 12 22 32	3 4 13 1- 23 2 33 3	4 5 4 15 4 25 4 35	6 16 26	7 17 20 37	8 (18) 28 38	 9 10 19 20 29 30 39 40 	support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can be
		S	Skill: 9 ti	imes table	1 11 21 31 41	2 12 22 32 42	3 4 13 1- 23 2 33 3 43 4	4 5 4 15 4 25 4 35 4 4	6 16 26 30 46	7 17 20 37 47	8 (38 48	 10 19 20 29 30 39 40 49 50 	support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can be supported using a
9	18	27	5kill: 9 ti	imes table	1 11 21 31 41 51	2 12 22 32 42 52	3 4 13 1 23 2 33 3 43 4 53 (5)	4 5 4 15 4 25 4 35 4 4 55	6 16 26 39 46 56	7 17 20 37 47 57	8 (28 38 48 58	 10 19 20 29 30 39 40 49 50 59 60 	support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a
9	18	27	5kill: 9 ti	imes table	1 11 21 31 41 51 61	2 12 22 32 42 52 62	3 4 13 1 23 2 33 3 43 4 53 5 6	4 5 4 15 4 25 4 35 4 65	6 16 26 46 56 66	7 17 20 37 47 57 67	8 (38 48 58 68	 10 19 20 29 30 39 40 49 50 59 60 69 70 	support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look
9 54	18 63	27 72	Skill: 9 ti 36 81	imes table	1 11 21 31 41 51 61 71	2 12 22 32 42 52 62 00	3 4 13 1 23 2 33 3 43 4 53 6 63 6 73 7	4 5 4 15 4 25 4 35 4 4 55 4 65 4 65 4 75	6 16 26 30 46 56 56 76	7 17 20 37 47 57 67 77	8 (19) 28 38 48 58 68 78	 10 19 20 29 30 39 40 49 50 59 60 69 70 79 80 	support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the nine
9 54	18 63	27 72	5kill: 9 ti 36 81	times table	1 11 21 31 41 51 61 71 (6)	2 12 22 32 42 52 62 62 82	3 4 13 1- 23 2 33 3 43 4 53 6 73 7 83 8	4 5 4 15 4 25 4 35 4 65 4 65 4 65 4 85	6 16 26 3 46 56 56 56 56 76 86	7 17 37 47 57 67 77 87	8 28 38 48 58 68 78 88	 10 19 20 29 30 39 40 49 50 59 60 69 70 80 89 60 	support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the nine times table, using concrete maninulatives
9 54	18 63	27 72	Skill: 9 ti 36 81	imes table	1 11 21 31 41 51 61 71 (6) 91	2 12 22 32 42 52 62 62 82 82 92	3 4 13 1 23 2 33 3 43 4 53 6 3 7 73 7 83 8 93 9	4 5 4 15 4 25 4 35 55 4 65 4 65 4 75 4 85 4 95	6 16 26 30 46 56 56 56 56 56 86 96	7 17 20 37 47 57 67 77 87 97	8 (28 38 48 58 68 78 88 98	 10 19 20 29 30 39 40 49 50 59 60 69 70 69 70 69 70 69 70 60 69 70 60 6	support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the nine times table, using concrete manipulatives
9 54	18 63	27 72	Skill: 9 ti 36 81	times table	1 11 21 31 41 51 61 71 (6) 91	2 12 22 32 42 52 62 82 92	3 4 13 1 23 2 33 3 43 4 53 6 3 6 73 7 83 8 93 9	4 5 4 15 4 25 4 35 4 35 55 4 65 4 65 4 85 4 95	6 16 26 30 46 56 56 56 56 86 96	7 17 37 47 57 67 77 87 97	8 28 38 48 58 68 78 88 98	9 10 19 20 29 30 39 40 49 50 59 60 69 70 79 80 89 60 99 100	support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the nine times table, using concrete manipulatives to support. Notice the pattern in the tens and
9 54	18 63	27 72	36 81	45 90	1 11 21 31 41 51 61 71 (6) 91	2 12 22 32 42 52 62 62 82 92	3 4 13 1 23 2 33 3 43 4 53 6 63 6 73 7 83 8 93 9	4 5 4 15 4 25 4 35 4 4 55 4 65 4 65 4 85 4 95	6 16 26 56 56 66 76 88 88 96	7 17 20 37 47 57 67 77 87 97	8 28 38 48 58 68 78 88 98	 10 19 20 29 30 29 30 40 49 50 60 69 70 69 70 69 70 89 60 69 100 	support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the nine times table, using concrete manipulatives to support. Notice the pattern in the tens and ones using the hundred
9 54	18 63	27 72	5kill: 9 ti 36 81	45 90	1 11 21 31 41 51 61 71 61 91	2 12 22 32 42 52 62 82 92	3 4 13 1 23 2 33 3 43 4 53 6 63 6 73 7 83 8 93 9 	4 5 4 15 4 25 4 35 4 65 4 65 4 65 4 85 4 95	6 16 26 30 46 56 66 76 86 86 96	7 17 37 47 57 67 77 87 97	8 28 38 48 58 68 78 88 98 98	 10 19 20 29 30 39 40 49 50 59 60 69 70 80 89 60 90 100 	support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the nine times table, using concrete manipulatives to support. Notice the pattern in the tens and ones using the hundred square to support as
9 54	18 63	27 72	36 81	45 90	1 11 21 31 41 51 61 71 61 71 91	2 12 22 32 42 52 62 (2) 82 92	3 4 13 1 23 2 33 3 43 4 53 6 63 6 73 7 83 8 93 9 	4 5 4 15 4 25 4 35 4 65 4 65 4 65 4 85 4 95	6 16 26 56 56 66 76 86 86 96	7 17 37 47 57 67 77 87 97	8 28 38 48 58 68 78 88 98 98	 10 19 20 29 30 29 30 40 49 50 60 69 70 80 89 90 100 	support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the nine times table, using concrete manipulatives to support. Notice the pattern in the tens and ones using the hundred square to support as well as noting the odd,
9 54	18 63	27 72	5kill: 9 ti 36 81	45 90	1 11 21 31 41 51 61 71 61 71 91	2 12 22 32 42 52 62 0 0 82 92	3 4 13 1. 23 2 33 3 43 4 53 6 63 6 73 7 83 8 93 9 93 9	4 5 4 15 4 25 4 35 4 65 4 65 4 65 4 85 4 95	6 16 26 56 66 76 86 86 96	7 17 37 47 57 67 77 87 97	8 28 38 48 58 68 78 88 98 98	 10 19 20 29 30 39 40 49 50 60 69 70 80 89 60 60 70 80 89 60 60 70 80 80 90 100 	support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the nine times table, using concrete manipulatives to support. Notice the pattern in the tens and ones using the hundred square to support as well as noting the odd, even pattern within the
9 54		27 72	Skill: 9 ti 36 81	45 90	1 11 21 31 41 51 61 71 91	2 12 22 32 42 52 62 0 0 92	3 4 13 1. 23 2 33 3 43 4 53 6 6 6 6 7 7 7 8 8 9 3 9 9 9 9 9 8 1	4 5 4 15 4 25 4 35 4 65 4 65 4 65 4 85 4 95	6 16 26 56 66 76 86 96	7 17 37 47 57 67 77 87 97	8 28 38 48 58 68 78 88 98 98	10 19 20 29 30 39 40 49 50 60 69 70 79 80 89 60 70 79 80 70 79 80 70	support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the nine times table, using concrete manipulatives to support. Notice the pattern in the tens and ones using the hundred square to support as well as noting the odd, even pattern within the multiples.

			Sk	kill: 7 tir	mes tab	le						Year 4
					1	2 3	4 5	6 🤇	8	9 10		Encourage daily
					11	12 13	15	16 17	18	19 20		counting in multiples
H				5	2	22 23	24 25	26 27	0	29 30		both forwards and
					31	32 33	34 🛞	36 37	38	39 40		backwards, supported
-	2005		-		41	42 43	44 45	46 43	48	19 50		by a number line or a
7	14	21	28	35	51	52 53	54 55	69 5	58	59 60		hundred square. The
42	49	56	63	70	61	62 🚯	64 65	66 6	68	69 🧭		seven times table car
		-			71	72 73	74 75	76 7	78	79 80		trickier to learn due t
					81	82 83	85	86 8	88	89 90		the lack of obvious
					9	92 93	94 95	96 9	99	99 100		pattern in the numbe
												however they already
-						~	~~	~~	~	20		know several facts du
-0	\mathcal{X}		<u> </u>		<i>m</i>)—	\odot		U	X)-	-	to commutativity.
												Children can still see
L.	а н	n a	E.	ав	3 1	ा	1	1	1	\rightarrow		odd, even pattern in
		_										
	7	14 2	28	35 42	49 5/	5 63	70	77 1	al.	-		multiples using numb
ò	7	14 2	28	35 42	49 50	5 63	70	א דל	34			multiples using numb shapes to support.
ò) 7	14 2	1 28 : Ski	35 42 ill: 11 ti	49 5 0	5 63 Die	70	א דל	, 34			multiples using numb shapes to support. Year 4
11	22	14 2' 33 4	1 28 3 Ski	35 42 ill: 11 ti	49 5 0 mes tab	5 63 ble	70	77 8	7 8	9 10]	multiples using numb shapes to support. Year 4 Encourage daily
11	22	14 2 33 4	1 28 5 Sk	35 42 ill: 11 ti 66	49 50	5 63 ole	1 70 4 5 14 15	6 16	7 8 17 18	9 10 19 20		multiples using numb shapes to support. Year 4 Encourage daily counting in multiples
11 77	22 88	14 2 33 4 99 11	1 28 Sk 4 55 0 121	35 42 ill: 11 ti 66 132	49 50 mes tak	2 3) 12 13 2 23	4 5 14 15 24 25	6 16 26	7 8 17 18 27 28	9 10 19 20 29 30		multiples using numb shapes to support. Year 4 Encourage daily counting in multiples both forwards and
11 77	22 88	14 2 33 4 99 11	Sk 4 55 0 121	35 42 ill: 11 ti 66 132	49 50 mes tab	5 63 De 2 3 12 13 23 32 (S)	4 5 14 15 24 25 34 35	6 16 26 5 36	7 8 17 18 27 28 37 38	9 10 19 20 29 30 39 40		multiples using numb shapes to support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can b
11 77	22 88	14 2 33 4 99 11	Sk 4 55 0 121	35 42 ill: 11 ti 66 132	49 50	2 3 12 13 22 3 12 13 23 32 3 42 43	4 5 14 15 24 25 34 35 45	6 16 26 36 36 36	7 8 17 18 27 28 37 38 47 48	9 10 19 20 29 30 39 40 49 50		multiples using numb shapes to support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can b supported using a
11 77	22 88	14 2 33 4 99 11	28 Sk 4 55 0 121	35 42 ill: 11 ti 66 132	49 50 mes tak	2 3 12 13 22 3 22 3 32 3 42 43 52 53	4 5 14 15 24 25 34 35 64 45 54 6	6 i 16 i 26 i 36 i 36 i 56	7 8 17 18 27 28 57 38 47 48 57 58	9 10 19 20 29 30 39 40 49 50 59 60		multiples using numb shapes to support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can b supported using a number line or a
11 77	22 88	14 2 33 4 99 11	28 Sk 4 55 0 121	35 42 ill: 11 ti 66 132	49 50 imes tak	2 3 12 13 22 3 12 13 23 23 42 43 52 53 62 63	4 5 14 15 24 25 34 35 54 5 64 65	6 16 26 36 46 56 56	7 8 17 18 27 28 57 38 47 48 57 58 57 68	9 10 19 20 29 30 39 40 49 50 59 60 69 70		multiples using numb shapes to support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can b supported using a number line or a hundred square. Lool
11 77	22 88	14 2 33 4 99 11	Sk 4 55 0 121	35 42 ill: 11 ti 66 132	49 50 mes tak	2 3 12 13 22 3 12 13 23 32 3 42 43 52 53 62 63 72 73	4 5 14 15 24 25 34 35 54 55 64 65 74 75	6 16 26 36 46 56 56 56 57 60	7 8 17 18 27 28 37 38 47 48 57 58 57 58 57 68 57 68	9 10 19 20 29 30 39 40 49 50 59 60 69 70 79 80		multiples using numb shapes to support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can b supported using a number line or a hundred square. Look for patterns in the
11 77	22 88	14 2 33 4 99 11 0 1 0 1 0 1	Sk 4 55 0 121	35 42 ill: 11 ti 66 132	49 50 imes tab	2 3 12 13 22 23 32 23 42 43 52 53 62 63 72 73 82 83	4 5 14 15 24 25 34 35 54 55 64 65 74 75 84 85	6 16 26 36 36 36 56 376 376	7 8 17 18 27 28 57 38 47 48 57 58 57 58 57 68 78 78 78	9 10 19 20 29 30 39 40 59 60 69 70 79 80 89 90		multiples using numb shapes to support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can k supported using a number line or a hundred square. Look for patterns in the eleven times table, us
11 77	22 88	14 2 33 4 99 11	Sk 4 55 0 121	35 42 ill: 11 ti 66 132	49 50 mes tak	2 3 12 13 22 23 12 13 22 23 32 33 42 43 52 53 62 63 72 73 82 83 92 93	4 5 14 15 24 25 34 35 64 65 74 75 84 85 94 95	6 16 26 36 46 5 6 76 6 76 6 6 76 5 6 6 76 6 76	7 8 17 18 27 28 37 38 47 48 57 58 57 68 57 78 38 39 39 98	9 10 19 20 29 30 39 40 49 50 59 60 59 60 79 80 89 90 90 10		multiples using numb shapes to support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can b supported using a number line or a hundred square. Look for patterns in the eleven times table, us concrete manipulativ
11 77	22 88	14 2 33 4 99 11 0 1	Sk 4 55 0 121	35 42 ill: 11 ti 66 132	49 50 mes tab	2 3 12 13 22 3 32 3 42 43 52 53 62 63 72 73 82 83 92 93	4 5 14 15 24 25 34 35 54 5 64 65 74 75 84 85 94 95	6 16 26 36 46 56 56 56 56 576 385 596	7 8 17 18 27 28 37 38 47 48 57 58 57 68 57 68 57 68 79 78 79 87 98	9 10 19 20 29 30 39 40 59 60 69 70 89 90 69 10		multiples using numb shapes to support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can b supported using a number line or a hundred square. Lool for patterns in the eleven times table, us concrete manipulative to support. Notice the
11 77	22 88	14 2 33 4 99 11 0 1	28 Sk 4 55 0 121	35 42 ill: 11 ti 66 132 0 1 0 1 0 1 0 1 0 1	49 50 mes tak	2 3 12 13 22 3 12 23 32 33 42 43 52 53 62 63 72 73 82 83 92 93	4 5 14 15 24 25 34 35 54 55 64 65 74 75 84 85 94 95	6 16 26 37 38 36 36 36 37 38 36 36 36 37 38 38 39 39 30	7 8 17 18 27 28 37 38 47 48 57 58 67 68 27 98 37 98	9 10 19 20 29 30 39 40 59 60 59 60 69 70 79 80 89 90 39 10		multiples using numb shapes to support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can b supported using a number line or a hundred square. Look for patterns in the eleven times table, us concrete manipulativ to support. Notice the pattern in the tens ar
	22 88	14 2 33 4 99 11	Sk 4 55 0 121	35 42 ill: 11 ti 66 132 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1	49 50 mes tak	2 3 12 13 22 23 32 23 42 43 52 53 62 63 72 73 82 83 92 93	4 5 14 15 24 25 34 35 54 5 64 65 74 75 84 85 94 95	6 16 26 36 46 56 56 6 86 396	7 8 17 18 27 28 37 38 37 38 37 38 37 38 37 38 37 98 37 98	9 10 19 20 29 30 39 40 49 50 59 60 69 70 79 80 89 90 90 10		multiples using numb shapes to support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can b supported using a number line or a hundred square. Look for patterns in the eleven times table, us concrete manipulativ to support. Notice the pattern in the tens ar ones using the hundr
	22 88	14 2 33 4 99 11 0 (28 Sk 4 55 0 121	35 42 ill: 11 ti 66 132 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1	49 50	2 3 12 13 22 23 32 23 42 43 52 53 62 63 72 73 82 83 92 93	4 5 14 15 24 25 34 35 54 55 64 65 74 75 84 85 94 95	6 16 26 36 46 56 6 86 96	7 8 17 18 27 28 37 38 47 48 57 58 57 68 67 68 67 68 67 68 67 98 67 98 67 98	9 10 19 20 29 30 39 40 59 60 69 70 89 90 10 10		multiples using numb shapes to support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can b supported using a number line or a hundred square. Look for patterns in the eleven times table, us concrete manipulativ to support. Notice the pattern in the tens ar ones using the hundr square to support. Al
	22 88	14 2 33 4 99 11 0 0 0 0 0 0 0 0 0 0 0 0 0	28 Sk 4 55 0 121	35 42 ill: 11 ti 66 132 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1	49 50 mes tak	2 3 12 13 22 23 12 13 22 23 32 23 42 43 62 63 72 73 82 83 92 93	4 5 14 15 24 25 34 35 54 55 64 65 74 75 84 85 94 95	6 16 26 36 46 56 6 6 76 6 76 6 76	7 8 17 18 27 28 37 38 37 38 37 48 57 58 57 68 57 68 57 68 57 68 57 68 57 98	9 10 19 20 29 30 39 40 49 50 59 60 59 60 69 70 79 80 89 90 69 10		multiples using numb shapes to support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can b supported using a number line or a hundred square. Look for patterns in the eleven times table, us concrete manipulativ to support. Notice the pattern in the tens ar ones using the hundr square to support. All consider the pattern
	22 88	14 2 33 4 99 11 0 (28 Sk 4 55 0 121	35 42 ill: 11 ti 66 132 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1	49 50 imes tak	2 3 12 13 22 23 32 23 42 43 52 53 62 63 72 73 82 83 92 93	4 5 14 15 24 25 34 35 54 5 64 65 74 75 84 85 94 95	6 16 26 36 36 36 36 36 376 386 396	7 8 17 18 27 28 57 38 57 38 57 48 57 68 57 68 57 68 57 68 57 68 57 68 57 98 57 98	9 10 19 20 29 30 39 40 49 50 59 60 69 70 79 80 89 90 69 10		multiples using numbers hapes to support. Year 4 Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Lood for patterns in the eleven times table, u concrete manipulative to support. Notice th pattern in the tens ar ones using the hundr square to support. Al consider the pattern after crossing 100



Multiplication

Skill	Year	Representations and Models				
Solve one-step problems with multiplication	1/2	Bar model Number shapes Counters	Ten frames Bead strings Number lines			
Multiply 2-digit by 1- digit numbers	3/4	Place value counters Base 10	Expanded written method Short written method			
Multiply 3-digit by 1- digit numbers	4	Place value counters Base 10	Short written method			
Multiply 4-digit by 1- digit numbers	5	Place value counters	Short written method			
Multiply 2-digit by 2- digit numbers	5	Place value counters Base 10	Short written method Grid method			
Multiply 2-digit by 3- digit numbers	5	Place value counters	Short written method Grid method			
Multiply 2-digit by 4- digit numbers	5/6	Formal written method				





Skill: Multiply 2-digit numbers by		Year 5						
20 2 ×								When multiplying a multi-digit number by 2-digits, use the area model to help children understand the size of the numbers they are using. This links to finding the area of a rectangle by finding
					H	т	0	the space covered by
	×	20	2			2	2	method matches the
	30	600	60	×		3	1	area model as an
	1	20	2			2	2	before moving on to
					6	6	0	the formal written
22 × 31 = 682]				6	8	2	multiplication method
Skill: Multiply 3-digit numbers by	2-digi	t num	bers					Year 5
	0			Th	ц.	т	0	Children can continue to use the area model
	0			m	2	1	4	when multiplying 3-
	X	56	X	~	2	2	2	digits by 2-digits. Place
	X				4	5	8	become more efficient
				7	0	2	0	to use but Base 10 can
		DC		7	4	8	8	the size of numbers.
		10						Children should now
								formal written
		×	200	30	כ	4	8	method, seeing the
		30	6,000	90	0	12	0	links with the grid
234 × 32 = 7,488		2	400	6	C	8		

Skill: Multiply 4-digit n	Year 5/6					
	TTh	Th	н	т	0	When multiplying 4- digits by 2-digits, children should be
		2	7	3	9	formal written
	×			2	8	still struggling with times tables, provide
	22	1 5	9 3	1	2	multiplication grids to support when they are focusing on the use of
	15	4	7 1	8	0	the method. Consider where exchanged
	7	6	6	9	2	digits are placed and make sure this is
			1			consistent
2,739 × 28	= 76,6	592	J			

Division

Below outlines the progressive steps within division, alongside the representations and models used to teach these.

Skills	Year	Representations and Models			
Solve one-step problems with division (sharing)	1/2	Bar model Real life objects	Arrays Counters		
Solve one-step problems	1/2	Real life objects Number	Arrays Counters		
with division (grouping)		shapes Bead strings Ten frames			
Divide 2-digits by 1- digit (no	3	Straws Base 10 Bar mode	Place value counters Part-		
exchange sharing)			whole model		
Divide 2-digits by 1- digit	3	Straws Base 10 Bar model	Place value counters Part-		
(sharing with exchange)			whole model		
Divide 2-digits by 1- digit	3/4	Straws Base 10 Bar model	Place value counters Part-		
(sharing with remainders)			whole model		
Divide 2-digits by 1- digit	4/5	Place value counters	Place value grid Written		
(grouping)		Counters	short division		
Divide 3-digits by 1- digit	4	Base 10 Bar model	Place value counters Part-		
(sharing with exchange)			whole model		
Divide 3-digits by 1- digit	4/5	Place value counters	Place value grid Written		
(grouping)		Counters	short division		
Divide 4-digits by 1- digit	5	Place value counters	Place value grid Written		
(grouping)		Counters	short division		
Divide multi-digits by 2-digits	6	Written short division	List of multiples		
(short division)					
Divide multi-digits by 2-digits	6	Written short division	List of multiples		
(long division)					









Skill: Divide 4-digits by 1-digit (grouping)	Year 5
$\boxed{\begin{array}{c} \hline h \\ \hline h \\ \hline \end{array} \\ \hline $ \\ \hline \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \\ \hline \end{array} \\ \hline \end{array} \\ \hline \\ \hline \\ \hline \end{array} \\ \hline \end{array} \\ \hline \\ \hline \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \\ \hline \\ \hline \\ \hline \end{array} \\ \hline \end{array} \\ \hline \\ \\ \\ \hline \\ \\ \\ \hline \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ } \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ } \\ \\ \\ \\ \\ \\ \\ \\ \\ } \\ \\ \\ \\ \\ \\ \\ \\ } \\ \\ \\ \\ } \\ \\ \\ \\ \\ \\ \\ \\ \\ } \\ \\ \\ \\ } \\ \\ } \\ \\ \\ \\ } \\ \\ } \\ \\ \\ \\ } \\ \\ \\ \\ } \\ \\ \\ } \\ \\ } \\ \\ \\ \\ } \\ \\ \\ \\ } \\ \\ } \\ \\ } \\ \\ \\ \\ } \\ } \\ \\ } \\ \\	Place value counters or plain counters can be used on a place value grid to support children to divide 4- digits by 1-digit. Children can also draw their own counters and group them through a more pictorial method. Children should be encouraged to move away from the concrete and pictorial when dividing numbers with multiple exchanges.
Skill: Divide multi digits by 2-digits (short division)	Year 6
Skill: Divide multi digits by 2-digits (short division)	Year 6
Skill: Divide multi digits by 2-digits (short division) $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Year 6 When children begin to divide up to 4- digits by 2-digits, written methods become the most accurate as concrete and pictorial representations
Skill: Divide multi digits by 2-digits (short division) Image: style="text-align: center;">Image: style="text-align: center;"	Year 6 When children begin to divide up to 4- digits by 2-digits, written methods become the most accurate as concrete and pictorial representations become less effective. Children can write out multiples to support their calculations with larger remainders. Children will also solve problems with remainders where the quotient can be rounded as appropriate.

Skill	kill: Divide multi-digits by 2-digits (long division)												Year 6			
1	2 -	0 4 3	3 6 3 2 6 0 7 2 7 2 0	(×30 (×6)	12 × 12 × 12 × 12 × 12 × 12 × 12 × 12 ×	1 = 2 = 3 = 5 = 7 = 7 = 7 = 10 =	12 24 36 48 60 72 84 96 108 = 12	3			43	52	÷	12	= 36	Children can also divide by 2- digit numbers using long division. Children can write out multiples to support their calculations with larger remainders. Children will also solve problems with remainders where the quotient can be
										0	4	8	9		W 422 424	rounded as appropriate.
									15	7	3	3	5		1 × 15 = 15	
-							-		-	б	0	a	0	(×400	$2 \times 15 = 30$	
	7.3	35	÷	15 =	48	89				1	3	3	5		3 × 15 = 45	
C		-	- 62 - 10				1		-	1	2	0	0	(×80)	$4 \times 15 = 60$	
											1	3	5	-	5 x 15 = 75	
									-		1	3	5	(×9)	$10 \times 15 = 150$	
													0			
Skill	Div	ide	multi	digits	s by 2	2-di	git	s (l	on	g d	ivis	ior	1 <i>,</i> W	vith r	emainders)	Year 6
						1				2	4	r	1	2	1 × 15 = 15	When a remainder is left at the end of a calculation, children
							1	5	3	7	2				$2 \times 15 = 30$	can either leave it as a
	•	47		~ 4	10			-	3	0	0				$3 \times 15 = 45$	remainder or convert it to a
31	2 -	- 13) =	24 r	12					7	2				$4 \times 15 = 60$	fraction. This will depend on the
								-		6	0				5 × 15 = 75	context of the question.
								-	-	1	2		-		$10 \times 15 = 150$	Children can also answer
										1.5	-					questions where the quotient
	Ĩ			2 4	4											needs to be rounded according

Monitoring and Review

This policy is reviewed biennially by the headteacher. Any changes or amendments to this policy will be communicated to all staff members by the headteacher. The scheduled review date for this policy is April 2026.